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7-1 Kinetic Energy (2 of 7)

- Energy is required for any sort of motion
- Energy:
 - Is a scalar quantity assigned to an object or a system of objects
 - Can be changed from one form to another
 - Is conserved in a closed system, that is the total amount of energy of all types is always the same
- In this chapter we discuss one type of energy (kinetic energy)
- We also discuss one method of transferring energy (work)

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7-1 Kinetic Energy (4 of 7)

Example

Sample Problem 7.01 Kinetic energy, train crash

In 1896 in Waco, Texas, William Crush parked two locomotives at opposite ends of a 6.4-km-long track, fired them up, tied their throttles open, and then allowed them to crash head-on at full speed (Fig. 7-1) in front of 30,000 spectators. Hundreds of people were hurt by flying debris; several were killed. Assuming each locomotive weighed 1.2×10^6 N and its acceleration was a constant 0.26 m/s², what was the total kinetic energy of the two locomotives just before the collision?

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7-1 Kinetic Energy (6 of 7)

Example Energy released by 2 colliding trains with given weight and acceleration from rest:

• Find the final velocity of each locomotive:

$$v^2 = v_0^2 + 2a(x - x_0).$$

 $v^2 = 0 + 2(0.26 \text{ m/s}^2)(3.2 \times 10^3 \text{ m}),$
 $v = 40.8 \text{ m/s} = 147 \text{ km/h}.$

• Convert weight to mass:

$$m = \frac{1.2 \times 10^6 \text{ N}}{9.8 \text{m/s}^2} = 1.22 \times 10^5 \text{kg}.$$

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7-2 Work and Kinetic Energy (5 of 16)

• Start from force equation and 1-dimensional velocity:

$$F_x = ma_x$$
, Equation (7-3)

$$v^2 = v_0^2 + 2a_x d.$$
 Equation (7-4)

• Rearrange into kinetic energies:

$$\frac{1}{2}mv^2 - \frac{1}{2}mv_0^2 = F_x d.$$
 Equation (7-5)

- The left side is now the change in energy
- Therefore, work is:

 $W = F_{\chi} d.$ Equation (7-6)

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7-2 Work and Kinetic Energy (6 of 16)

To calculate the work a force does on an object as the object moves through some displacement, we use only the force component along the object's displacement. The force component perpendicular to the displacement does zero work.

• For an angle ϕ between force and displacement:

 $W = Fd \cos \phi$ Equation (7-7) As vectors we can write: $W = \vec{F} \cdot \vec{d}$ Equation (7-8)





7-2 Work and Kinetic Energy (9 of 16)

A force does positive work when it has a vector component in the same direction as the displacement, and it does negative work when it has a vector component in the opposite direction. It does zero work when it has no such vector component.

- For two or more forces, the **net work** is the sum of the works done by all the individual forces
- Two methods to calculate net work:
 - We can find all the works and sum the individual work terms.
 - $\,\circ\,$ We can take the vector sum of forces $(F_{\rm net})$ and calculate the net work once

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7-2 Work and Kinetic Energy (12 of 16)

Checkpoint 1

A particle moves along an x axis. Does the kinetic energy of the particle increase, decrease, or remain the same if the particle's velocity changes (a) from -3 m/s to -2 m/s and (b) from -2 m/s to 2 m/s? (c) In each situation, is the work done on the particle positive, negative, or zero?

Answer:

(a) energy decreases

- (b) energy remains the same
- (c) work is negative for (a), and work is zero for (b)

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Work done by two constant forces, industrial spies

Figure 7-4*a* shows two industrial spies sliding an initially stationary 225 kg floor safe a displacement \vec{d} of magnitude 8.50 m. The push \vec{F}_1 of spy 001 is 12.0 N at an angle of 30.0° downward from the horizontal; the pull \vec{F}_2 of spy 002 is 10.0 N at 40.0° above the horizontal. The magnitudes and directions of these forces do not change as the safe moves, and the floor and safe make frictionless contact.



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7-2 Work and Kinetic Energy (16 of 16) **Work done by two constant forces, industrial spies** (c) The safe is initially stationary. What is its speed v_f at the end of the 8.50 m displacement? **Calculations:** We relate the speed to the work done by combining Eqs. 7-10 (the work-kinetic energy theorem) and r-1 (the definition of kinetic energy): $W = K_f - K_i = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$. The initial speed v_i is zero, and we now know that the work done is 153.4 J. Solving for v_f and then substituting known data, we find that $v_f = \sqrt{\frac{2W}{m}} = \sqrt{\frac{2(153.4 \text{ J})}{225 \text{ kg}}} = 1.17 \text{ m/s}.$ (Answer)







7-3 Work Done by the Gravitational Force (4 of 8)

• Work done in lifting or lowering an object, applying an upwards force:

$$\Delta K = K_f - K_i = W_a + W_g,$$
 Equation (7-15)

- For a stationary object:
 - Kinetic energies are zero
 - We find:

$$\begin{array}{l} W_a + W_g = 0 \\ W_a = -W_g. \end{array}$$

Equation (7-16)





















7-4 Work Done by a Spring Force (7 of 13)• We can find the work by integrating: $W_s = \int_{x_i}^{x_f} -F_x dx.$ Equation (7-23)• Plug kx in for F_x : $W_s = \frac{1}{2}kx_i^2 - \frac{1}{2}kx_f^2$ Equation (7-25)• The work:• Can be positive or negative• Depends on the net energy transfer

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7-4 Work Done by a Spring Force (8 of 13)

Work W_s is positive if the block ends up closer to the relaxed position (x = 0) than it was initially. It is negative if the block ends up farther away from x = 0. It is zero if the block ends up at the same distance from x = 0.

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7-4 Work Done by a Spring Force (9 of 13)

• For an initial position of *x* = 0:

$$W_s = -\frac{1}{2}kx^2$$
 Equation (7-26)

• For an applied force where the initial and final kinetic energies are zero:

$$W_a = -W_s$$
. Equation (7-28)

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If a block that is attached to a spring is stationary before and after a displacement, then the work done on it by the applied force displacing it is the negative of the work done on it by the spring force.

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7-5 Work Done by a General Variable Force (5 of 5)

Work, two-dimensional integration

Force $\vec{F} = (3x^2 N)\hat{i} + (4 N)\hat{j}$, with x in meters, acts on a particle, changing only the kinetic energy of the particle. How much work is done on the particle as it moves from coordinates (2 m, 3 m) to (3 m, 0 m)? Does the speed of the particle increase, decrease, or remain the same?

Calculation: We set up two integrals, one along each axis:

$$W = \int_{2}^{3} 3x^{2} dx + \int_{3}^{0} 4 dy = 3 \int_{2}^{3} x^{2} dx + 4 \int_{3}^{0} dy$$

= $3[\frac{1}{3}x^{3}]_{2}^{3} + 4[y]_{3}^{0} = [3^{3} - 2^{3}] + 4[0 - 3]$
= 7.0 J. (Answer)

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7-6 Power (4 of 5) • Solve for the instantaneous power using the definition of work: $P = \frac{dW}{dt} = \frac{F \cos \phi \, dx}{dt} = F \cos \phi \left(\frac{dx}{dt}\right),$ $P = Fv \cos \phi. \qquad \text{Equation (7-47)}$ • Or: $P = \vec{F} \cdot \vec{v} \qquad \text{Equation (7-48)}$





Summary (2 of 6)	
Work Done by a Constant Force	
$W = Fd\cos\phi$	Equation (7-7)
$W = ec{F} \cdot ec{d}$	Equation (7-8)
• The net work is the sum of individual works	
Work and Kinetic Energy	
$\Delta K = K_f - K_i = W,$	Equation (7-10)
$K_f = K_i + W,$	Equation (7-11)
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Summary (6 of 6)	
• Instantaneous power:	
$P = \frac{dW}{dt}$	Equation (7-43)
• For a force acting on a moving object:	
$P=F\nu\cos\phi.$	Equation (7-47)
$P=ec{F}\cdotec{ u}$	Equation (7-48)
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