

15-1 Simple Harmonic Motion (1 of 20)

Learning Objectives

- **15.01** Distinguish simple harmonic motion from other types of periodic motion.
- **15.02** For a simple harmonic oscillator, apply the relationship between position x and time t to calculate either if given a value for the other.

15.03 Relate period *T*, frequency *f*, and angular frequency ω .















15-1 Simple Harmonic Motion (9 of 20) • The **frequency** of an oscillation 1 cycle is the number of times per +Asecond that it completes a full oscillation (cycle) • Unit of hertz: 1 Hz = 1oscillation per second • The time in seconds for one full cycle is the **period** -A $T = \frac{1}{f}$ Equation (15-2) Period = TCopyright ©2018 John Wiley & Sons, Inc 10







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Checkpoint 1

A particle undergoing simple harmonic oscillation of period *T* (like that in Fig. 15-2) is at $-x_m$ at time t = 0.

Is it at $-x_m$, at $+x_m$, at 0, between $-x_m$ and 0, or between 0 and $+x_m$ when

(a) t = 2.00T, (b) t = 3.50T, and (c) t = 5.25T?

Answer:

- (a) at $-x_m$
- (b) at x_m
- (c) at 0

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In SHM, the acceleration a is proportional to the displacement x but opposite in sign, and the two quantities are related by the square of the angular frequency ω

Checkpoint 2

Which of the following relationships between a particle's acceleration a and its position x indicates simple harmonic

oscillation: (a) $a = 3x^2$, (b) a = 5x, (c) a = 4x, (d) $a = \frac{-2}{x}$?

For the SHM, what is the angular frequency (assume the unit of rad/s)?

Answer:

(c) where the angular frequency is 2

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Checkpoint 3

Which of the following relationships between the force *F* on a particle and the particle's position *x* gives SHM: (a) F = -5x,

(b) $F = -400x^2$, (c) F = 10x, (d) $F = 3x^2$?

Answer:

only (a) is simple harmonic motion (note that b is harmonic motion, but nonlinear and not SHM)

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Resonance (1 of 7)

Learning Objectives

- **15.43** Distinguish between natural angular frequency and driving angular frequency.
- **15.44** For a forced oscillator, sketch a graph of the oscillation amplitude versus the ratio of the driving angular frequency to the natural angular frequency, identify the approximate location of resonance, and indicate the effect of increasing the damping.
- **15.45** For a given natural angular frequency, identify the approximate driving angular frequency that gives resonance.

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Summary (1 of 5)	
Frequency	
• $1 \text{ Hz} = 1 \text{ cycle per second}$	
Period	
$T = \frac{1}{f}.$	Equation (15-2)
Simple Harmonic Motion	
• Find <i>v</i> and <i>a</i> by differentiation	
$x(t) = x_m \cos(\omega t + \phi)$	Equation (15-3)
$\omega = \frac{2\pi}{T} = 2\pi f.$	Equation (15-5)
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